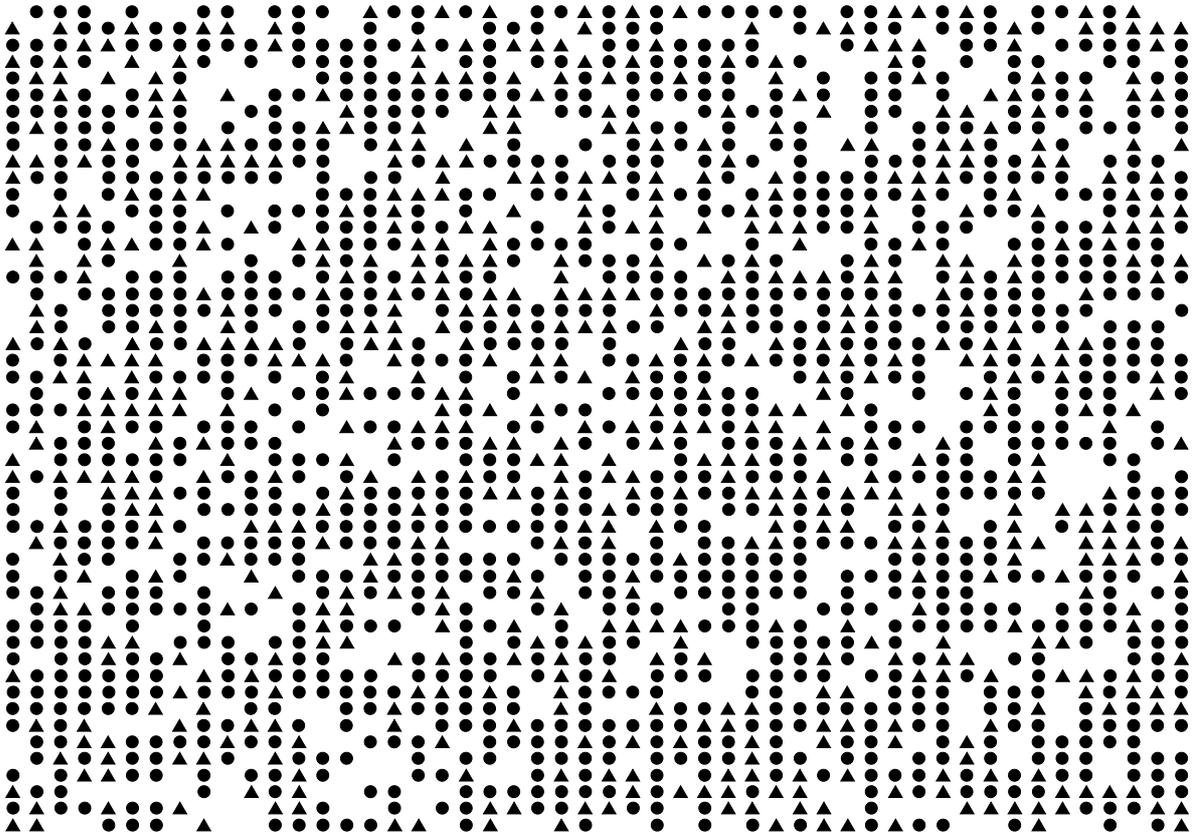


Counting Trees



This diagram shows some trees in a plantation.

The circles ● show old trees and the triangles ▲ show young trees.

Tom wants to know how many trees there are of each type, but says it would take too long counting them all, one-by-one.

1. What method could he use to estimate the number of trees of each type?
Explain your method fully.
2. On your worksheet, use your method to estimate the number of:
 - (a) Old trees
 - (b) Young trees

Follow-up task for students

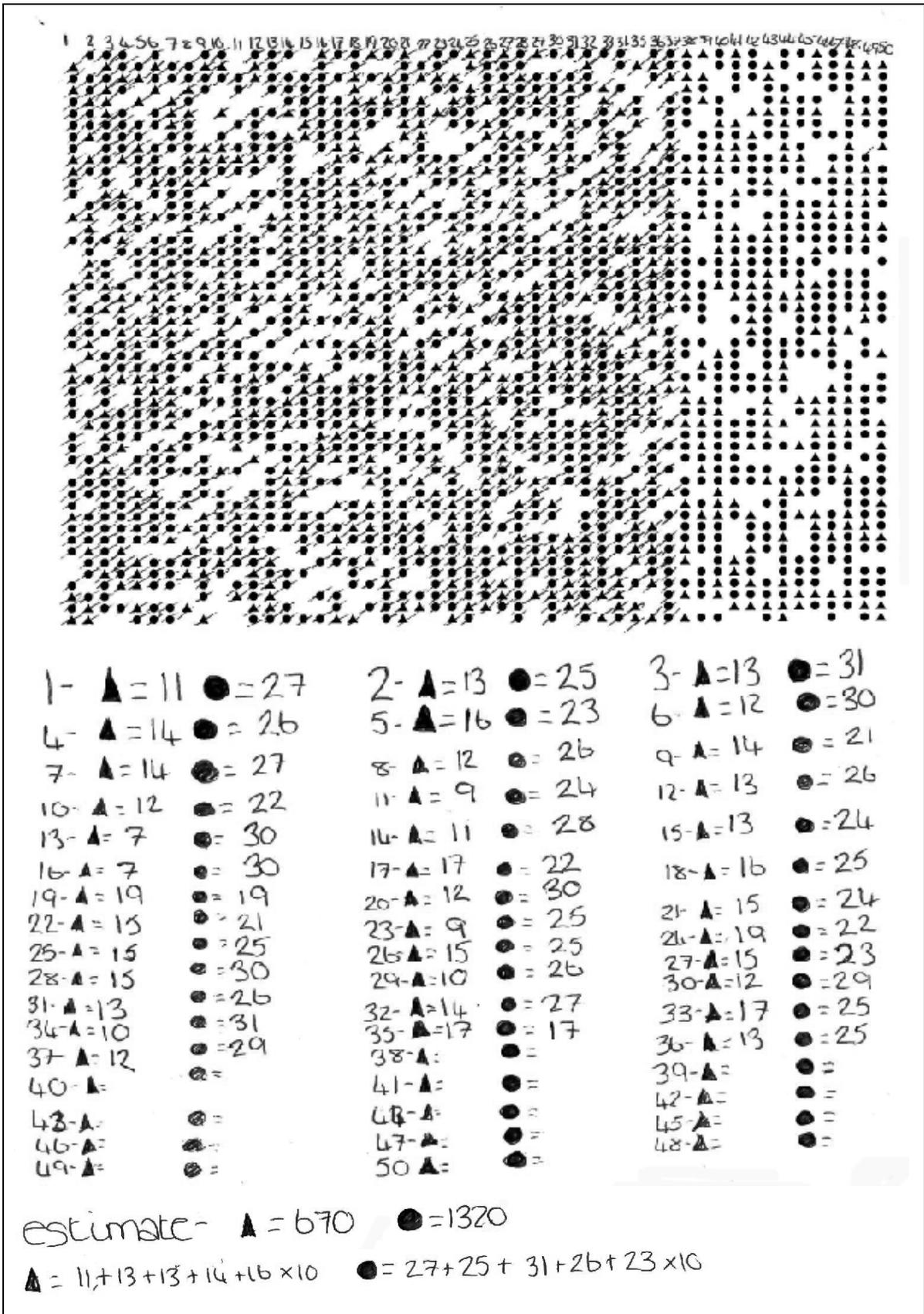
Look carefully at the following extracts of work from other students. Imagine you are their teacher. Go through each piece of work and write comments on each one.

- Have they chosen a sensible method?
- Are the calculations correct?
- Are the conclusions sensible?
- Is the work easy to understand?

Name	Comments
Sarah	
Laura	
Jenny	
Woody	
Amber	

Now try to write out an answer that is better than all of them!

Sample response: Sarah



Sample response: Laura

① You could multiply the number of trees in the length by the number of trees in the width and then half your answer.

② a. Old trees - 644
Young trees - 644

width - 33 $33 \times 39 = 1287$
length - 39 $1287 \div 2 = 643.5 = 644$

Sample response: Jenny

1. there are 38 trees in each column
there are around 11 young trees
and around 27 old ones
33 trees in each row so

$$\begin{array}{r} 11 \times 33 = 363 \\ 27 \times 33 = \underline{891} \\ \hline 1254 \end{array}$$

2.

a. $11 \times 33 = 363 = \text{new trees.}$

b. $27 \times 33 = 891 = \text{old trees.}$

Sample response: Woody

2 columns has 21 young trees
55 old trees

50 columns is approx
 $50 \div 2 = 25$
 $25 \times 21 =$ amount of young trees $= 525$
 $25 \times 55 =$ amount of old trees $= 1,375$
rounded up

young 530
old 1,380

Sample response: Amber

Counting trees

1. If Tom draws a 10x10 square round some trees and counts how many old and new there are. There are 50 rows and 50 columns altogether so he must multiply by 25. He could do this a few times to check and then take the average.
- 2.

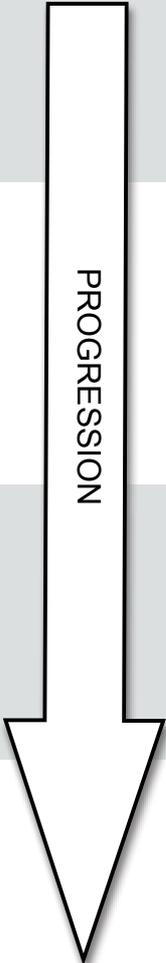
53 old	$\times 25 =$	1325 old	
28 new	$\times 25 =$	700 new	
19 spaces	$\times 25 =$	475 spaces	
<u>100</u>		<u>2500</u>	

$1325 + 700 \div 2 = 1262.5$
 $700 + 875 \div 2 = 787.5$

check

48 old	$\times 25 =$	1200 old	So about 1263 old trees and 788 new trees
35 new	$\times 25 =$	875 new	
17 spaces	$\times 25 =$	425 spaces	
<u>100</u>		<u>2500</u>	

Progression in key processes

	Representing	Analysing	Interpreting and evaluating	Communicating and reflecting
 PROGRESSION	<p>Chooses a method, but this may not involve sampling.</p> <p>E.g. Counts all trees or multiplies the number of trees in a row by the number in a column.</p>	<p>Follows chosen method, possibly making errors.</p> <p>E.g. Does not account for different numbers of old and young trees or that there are gaps.</p>	<p>Estimates number of new and old trees, but answer given is unreasonable due to method and errors.</p>	<p>Communicates work adequately but with omissions.</p>
	<p>Chooses a sampling method but this is unrepresentative or too small.</p> <p>E.g. tries to count the trees in first row and multiplies by the number of rows.</p>	<p>Follows chosen method, mostly accurately.</p> <p>E.g. May not account for different numbers of old and young trees or that there are gaps.</p>	<p>Estimates number of new and old trees, but answer given is unreasonable due mainly to the method.</p>	<p>Communicates reasoning and results adequately, but with omissions.</p>
	<p>Chooses a reasonable sampling method.</p>	<p>Follows chosen method, mostly accurately.</p>	<p>Estimates a reasonable number of old and new trees in the plantation.</p> <p>The reasonableness of the estimate is not checked. E.g. by repeating with a different sample.</p>	<p>Explains what they are doing but explanation may lack detail.</p>
	<p>Chooses an appropriate sampling technique.</p>	<p>Follows chosen method accurately.</p> <p>Uses a proportional argument correctly.</p>	<p>Deduces a reasonable number of old and new trees in the plantation.</p> <p>There is some evidence of checking the estimate. E.g. Considers a different sampling method.</p>	<p>Communicates reasoning clearly and fully.</p>